

## Nuclear Theory - Course 227

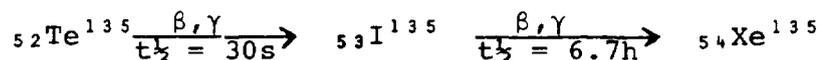
## FISSION PRODUCT POISONING

All Fission products can be classified as reactor poisons because they all absorb neutrons to some extent. Most simply buildup slowly as the fuel burns up and are accounted for as a long term reactivity effect (as we did in lesson 227.00-7). However, two of the fission products, Xe-135 and Sm-149, are significant by themselves due to their absorption cross section and high production as fission products or fission product daughters. Xenon-135 has a microscopic absorption cross section of  $3.5 \times 10^6$  barns and a total fission product yield of 6.6%. Samarium-149 has an absorption cross section of 42,000 barns and a total fission product yield of 1.4%. Xenon-135 is the more important of the two and will be dealt with in more detail.

Xenon-135

Xenon-135 (often carelessly referred to just as xenon) is produced in the fuel in two ways:

- a) Directly from fission. About 0.3% of all fission products are Xe-135.
- b) Indirectly from the decay of iodine-135, which is either produced as a fission product or from the decay of the fission product tellurium-135 via the following decay chain:



Te-135 and I-135 together constitute about 6.3% of all fission products. Due to the short half-life of Te-135 we normally consider the whole 6.3% to be produced as I-135. The rate of production of xenon and iodine from fission depends on the fission rate. Thus:

Rate of production  
of Xe-135 from fission =  $\gamma_{\text{Xe}} \Sigma_f \phi$

$$\text{Rate of production of I -135 from fission} = \gamma_I \Sigma_f \phi$$

- where:  $\gamma_{Xe}$  = Fission product yield of Xe  
 $\gamma_I$  = Fission product yield of I  
 $\Sigma_f$  = Microscopic fission cross section  
 $\phi$  = Average thermal neutron flux

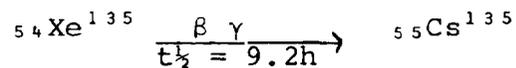
The rate of production of xenon from iodine depends only on the decay of the iodine, thus:

$$\text{Rate of production of Xe -135 from I -135} = \lambda_I N_I$$

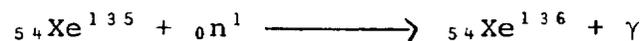
- where:  $\lambda_I$  = decay constant for I -135 ( $S^{-1}$ )  
 $N_I$  = concentration of I -135 ( $\frac{\text{atoms}}{\text{cm}^3}$ )

Xenon-135 is removed (or changed) by two processes:

- a) Radioactive decay as follows:



- b) Neutron absorption (burnout):



Niether Cs -135 nor Xe -136 are significant neutron absorbers. The removal rates are as follows:

$$\text{Rate of change of Xe -135 by decay} = \lambda_{Xe} N_{Xe}$$

$$\text{Rate of change of Xe -135 by burnout} = \sigma_a^{Xe} N_{Xe} \phi$$

- where:  $\lambda_{Xe}$  = decay constant for Xe -135  
 $N_{Xe}$  = Concentration of Xe -135  
 $\sigma_a^{Xe}$  = microscopic absorption cross section  
 $\phi$  = thermal neutron flux

Now we can set up two equations, one which describes the behaviour of xenon and one which describes the behaviour of iodine. The time rate of change of the iodine ( $\frac{dN_I}{dt}$ ) is:

$$\frac{d}{dt} N_I = \underbrace{\gamma_I \Sigma_f \phi}_{\text{Production from fission}} - \underbrace{\lambda_I N_I}_{\text{Loss due to decay}} \quad (1)$$

The time rate of changes of the xenon ( $\frac{d}{dt} N_{Xe}$ ) is:

$$\frac{d}{dt} N_{Xe} = \underbrace{\gamma_{Xe} \Sigma_f \phi}_{\text{Production from fission}} + \underbrace{\lambda_I N_I}_{\text{Production from the decay of Iodine}} - \underbrace{\lambda_{Xe} N_{Xe}}_{\text{Loss due to decay}} - \underbrace{\sigma_a^{Xe} N_{Xe} \phi}_{\text{Loss due to burnup}} \quad (2)$$

We would like to examine the buildup of xenon in the reactor; however, since much of the xenon comes from iodine we must examine the behaviour of iodine first.

Examining equation (1) you can see that if we startup a reactor with no iodine present we will initially have a production term ( $\gamma_I \Sigma_f \phi$ ) but no loss term since  $N_I$  is zero. As iodine is created the loss term grows ( $N_I$  is increasing) while production term remains constant (for constant power). Eventually the loss will equal the production and the iodine level will remain constant. Mathematically:

$$\frac{d}{dt} N_I = 0 = \gamma_I \Sigma_f \phi - \lambda_I N_I$$

$$\lambda_I N_I = \gamma_I \Sigma_f \phi$$

$$\underbrace{N_I}_{\text{Equilibrium iodine concentration}} = \frac{\gamma_I \Sigma_f \phi}{\lambda_I}$$

Equilibrium iodine concentration.

This is a simple exponential buildup which can be considered to reach equilibrium after about five half-lives or 30 hours (within 3%). The buildup is shown in Figure 1.

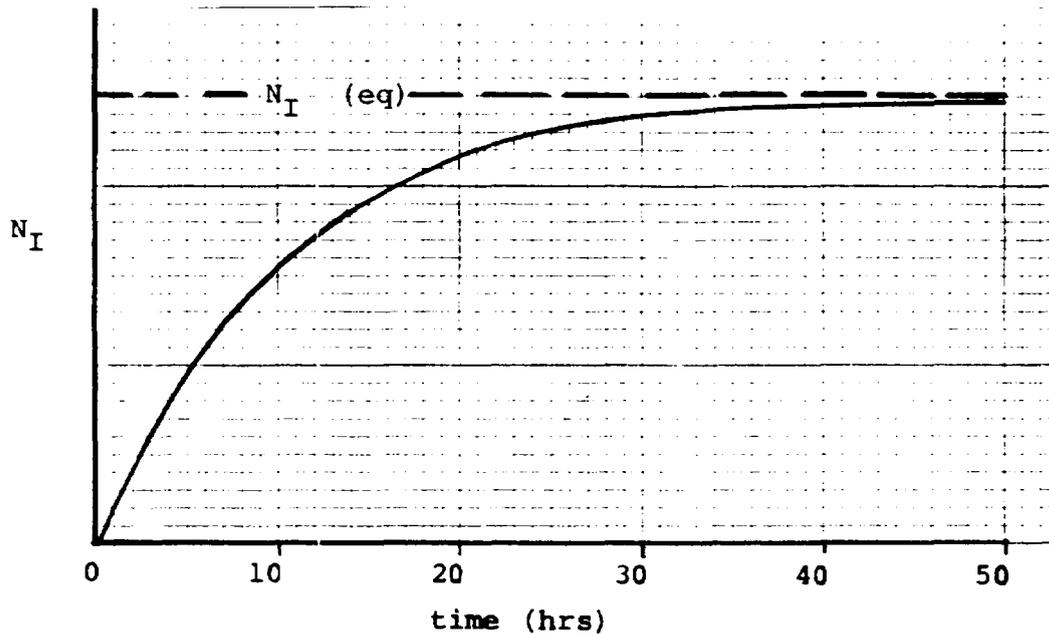


Figure 1

Now we are able to examine the behaviour of xenon. The buildup of xenon is somewhat more complex than the buildup of iodine. Again at equilibrium,  $\frac{d}{dt} N_{Xe} = 0$ , and production equals loss. Also iodine must be in equilibrium so  $\gamma_I \Sigma_f \phi = \lambda_I N_I$ . Thus we can write:

$$\gamma_{Xe} \Sigma_f \phi + \gamma_I \Sigma_f \phi = \lambda_{Xe} N_{Xe} + \sigma_a^{Xe} N_{Xe} \phi \quad (3)$$

Rearranging:

$$\underbrace{N_{Xe}}_{\text{Equilibrium Xe concentration}} = \frac{(\gamma_{Xe} + \gamma_I) \Sigma_f \phi}{\lambda_{Xe} + \sigma_a^{Xe} \phi}$$

The buildup is shown graphically in Figure 2.

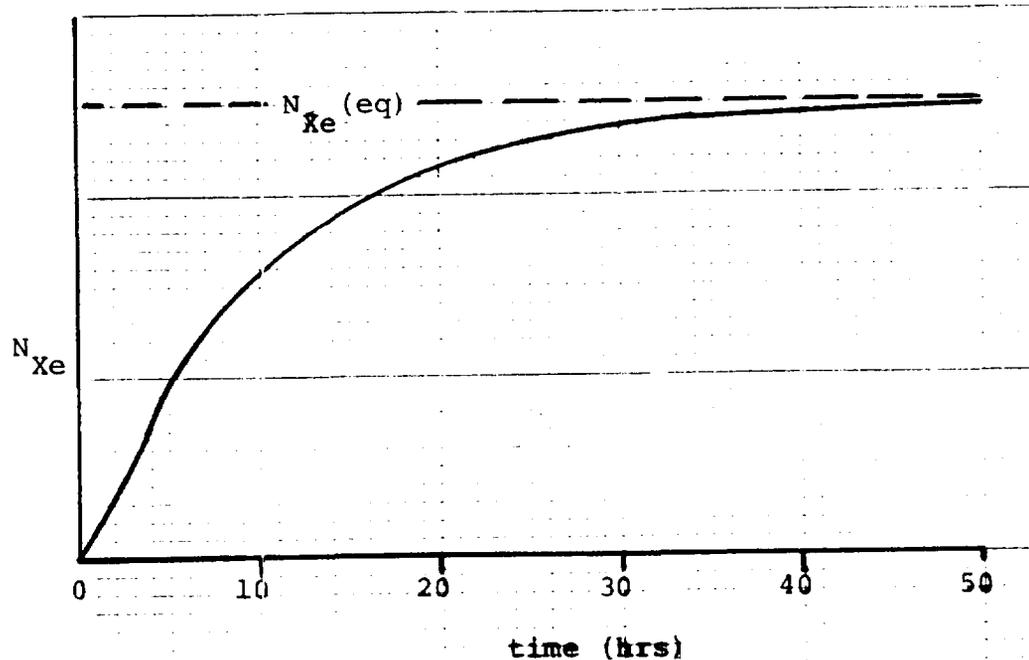


Figure 2

It again takes about 5 half-lives to reach equilibrium and for xenon this is about 50 hours.

It is useful to know the relative importance of the production and loss terms for xenon at equilibrium. Examining equation (3) we see the relative importance of the production terms depend only on their respective fission product yields. Thus direct production of Xe-135 from fission is about 5% of the total production at equilibrium while indirect production from the decay of I-135 is 95% of the total production.

In examining the loss terms, note that the loss due to decay depends only on the decay constant ( $\lambda_{Xe}$ ). The loss due to burnout depends on the cross section ( $\sigma_a^{Xe}$ ) and the neutron flux. Therefore, the relative importance of the loss terms varies from reactor to reactor depending on the normal flux levels. For a given reactor the relative importance varies with power level. For our larger reactors (Bruce and Pickering) full power flux is  $7 \times 10^{13} \frac{n-cm}{cm^3 s}$

$$\begin{aligned} \text{Thus; } \lambda_{Xe} &= 2.1 \times 10^{-5} \text{ s}^{-1} \\ \sigma_a^{Xe} &= 24.5 \times 10^{-5} \text{ s}^{-1} \end{aligned}$$

Therefore, burnout constitutes more than 90% of the loss at full power.

### Reactivity

The reactivity worth of xenon (called Xenon Load) is a function of the concentration of xenon. As it is the reactivity due to xenon that we are concerned about, it is normal to express Xenon Load in reactivity units ( $\Delta k_{Xe}$ ). As shown in Figure 3, the equilibrium Xenon Load for 100% is about -28 mk.

It is also common practice to express the concentration of iodine as Iodine Load in mk. It is important to realize that iodine is not itself a poison hence there is no actual reactivity associated with it. *Iodine Load* is by definition the reactivity if all the iodine present were instantaneously changed to xenon. I repeat it is not an actual reactivity.

By examining the equations for equilibrium xenon and iodine it can be deduced that equilibrium Iodine Load is a direct function of power (eg, doubling the power doubles the Iodine Load) whereas equilibrium Xenon Load does not have such a straightforward relationship with power. Figure 3 shows the approximate variation of equilibrium Xenon Load with power for Bruce or Pickering. The significant point is that equilibrium Xenon Load doesn't change much over the normal operating range.

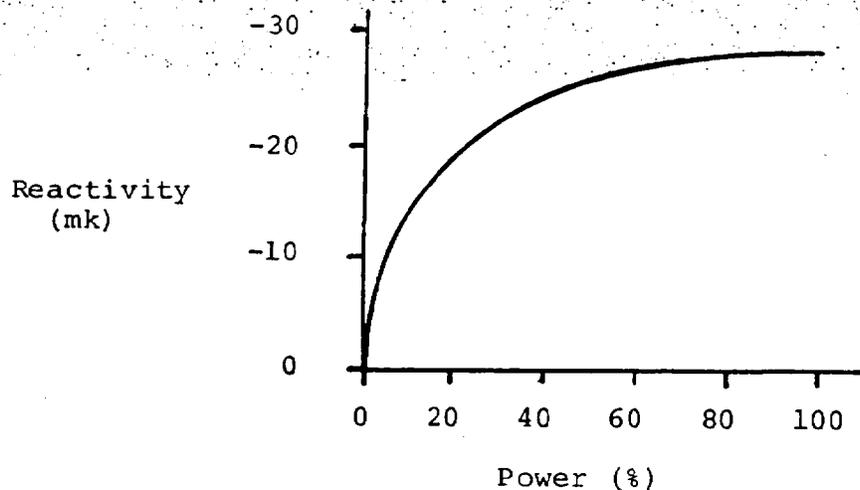


Figure 3

### Xenon Simulation

The reactivity due to Equilibrium Xenon is easily compensated for by designing the reactor to have sufficient excess positive reactivity to overcome the negative reactivity due to the xenon. Now the regulating system must be capable of controlling the excess positive reactivity when there is no xenon present (eg, startup after a long shutdown). This is most commonly done by dissolving a poison (boron or gadolinium) in the moderator and removing it as the xenon builds up. This addition of poison to the moderator on startup is called Xenon Simulation.

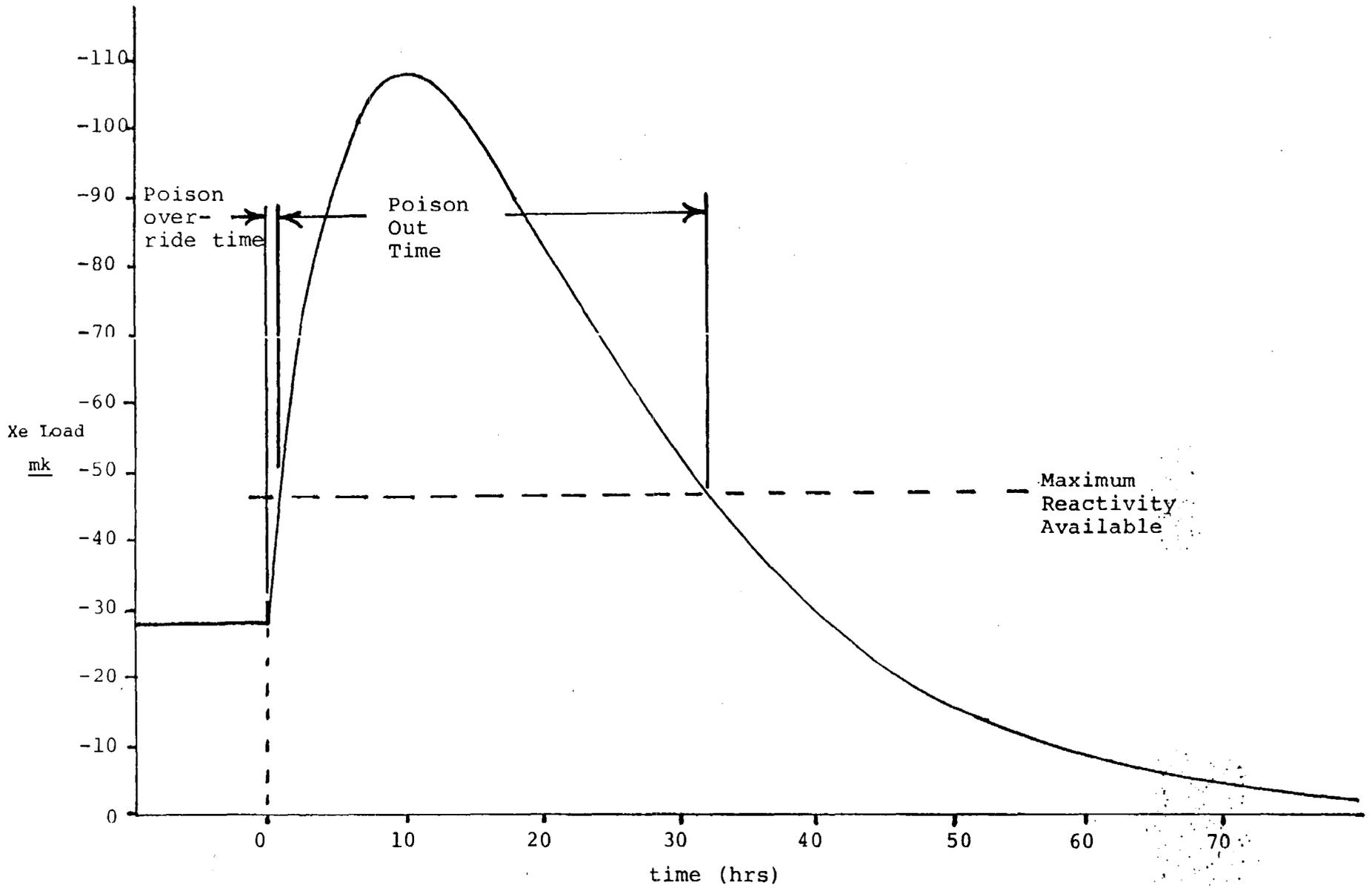
As you may suspect, the buildup to and presence of Equilibrium Xenon does not present a significant problem in the operation of our reactors. However, the transient behaviour of xenon creates a major obstacle to operation.

### Transient Xenon Behaviour

Assume a reactor has been operating at 100% power long enough for xenon to have reached equilibrium. If power is rapidly reduced to essentially 0%, what happens to the xenon concentration? To answer this question we shall examine the differential equation which describes the time behaviour of xenon.

$$\frac{dN_{Xe}}{dt} = \underbrace{\gamma_{Xe} \Sigma_f \phi}_{5\%} + \underbrace{\gamma_I N_I}_{95\%} - \underbrace{\gamma_{Xe} N_{Xe}}_{10\%} - \underbrace{\sigma_a N_{Xe} \phi}_{90\%}$$

The percentages shown are the relative magnitudes of the production and loss terms prior to the decrease in power. When power is reduced to 0%, the small production term ( $\gamma_{Xe} \Sigma_f \phi$  - direct fission production) and the large loss term ( $\sigma_a N_{Xe} \phi$  - burnup) both cease. Since the major production term ( $\lambda_I N_I$  - decay of iodine) continues the concentration of xenon starts to increase. The increase can't go on forever since there is a limited supply of iodine, thus the xenon peaks and eventually decays away. This is shown graphically in Figure 4.



Behaviour of Xenon Load after a trip from full power.

Figure 4

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The height of the peak above the equilibrium load turns out to be almost directly proportional to the flux before the trip, providing that equilibrium conditions had been set up by them. Consequently, although the equilibrium xenon loads differ only marginally for our reactors, the xenon transients do not. They are roughly the same for Pickering, Douglas Point, and Bruce with a transient peak about 80 mk above the equilibrium xenon load. At NPD it is merely 22 mk. The different values are due to the different fluxes in these reactors.

The rate of rise of the xenon load after a trip is also a function of the equilibrium conditions before the trip. In our reactors, it is typically around 24 mk per hour for a trip from full power. If a reactor has a maximum available reactivity of, say, 18 mk, you can see that it must be brought back to full power within 45 minutes (the *poison override time*) to burn the xenon out, otherwise it wouldn't be possible to start up again until the xenon transient has passed through its peak and decayed. If this happens, the reactor is said to have *poisoned out*. The *poison out time* may be as high as 32 hours. Obviously, this represents a loss of 32 hours worth of power production.

The desired reactivity for poison override may be provided in a number of ways. The most common are to either remove *adjusters* normally in the core, or to insert *boosters* into the core. Designing a reactor to have a longer override time than is needed costs money; in the first case as reduced fuel burnup and in the second as increased capital cost. In practice the cost of providing the excess reactivity is usually optimized with respect to the energy production that would otherwise have been lost during the poison out time.

So far, we have only discussed the xenon transients occurring after a shutdown from full power equilibrium conditions. In practical reactor operation, we are also interested in the transients after a shutdown from less than full power, and after a step reduction in power. Solving the corresponding xenon equations is a laborious chore and computer codes are normally used. Figures 5, 6, and 7 show the results of such calculations for Douglas Point, for example. These results were taken from the Douglas Point Design Manual, and as far as can be ascertained, they appear to be essentially in agreement with what happens there in practice.

Fig. 5 - shows the transients for 20, 40, 50, 80 and 100% power reductions from initial full power. For a reduction of, say, 40% (ie, from 200  $\rightarrow$  120 MW), the xenon

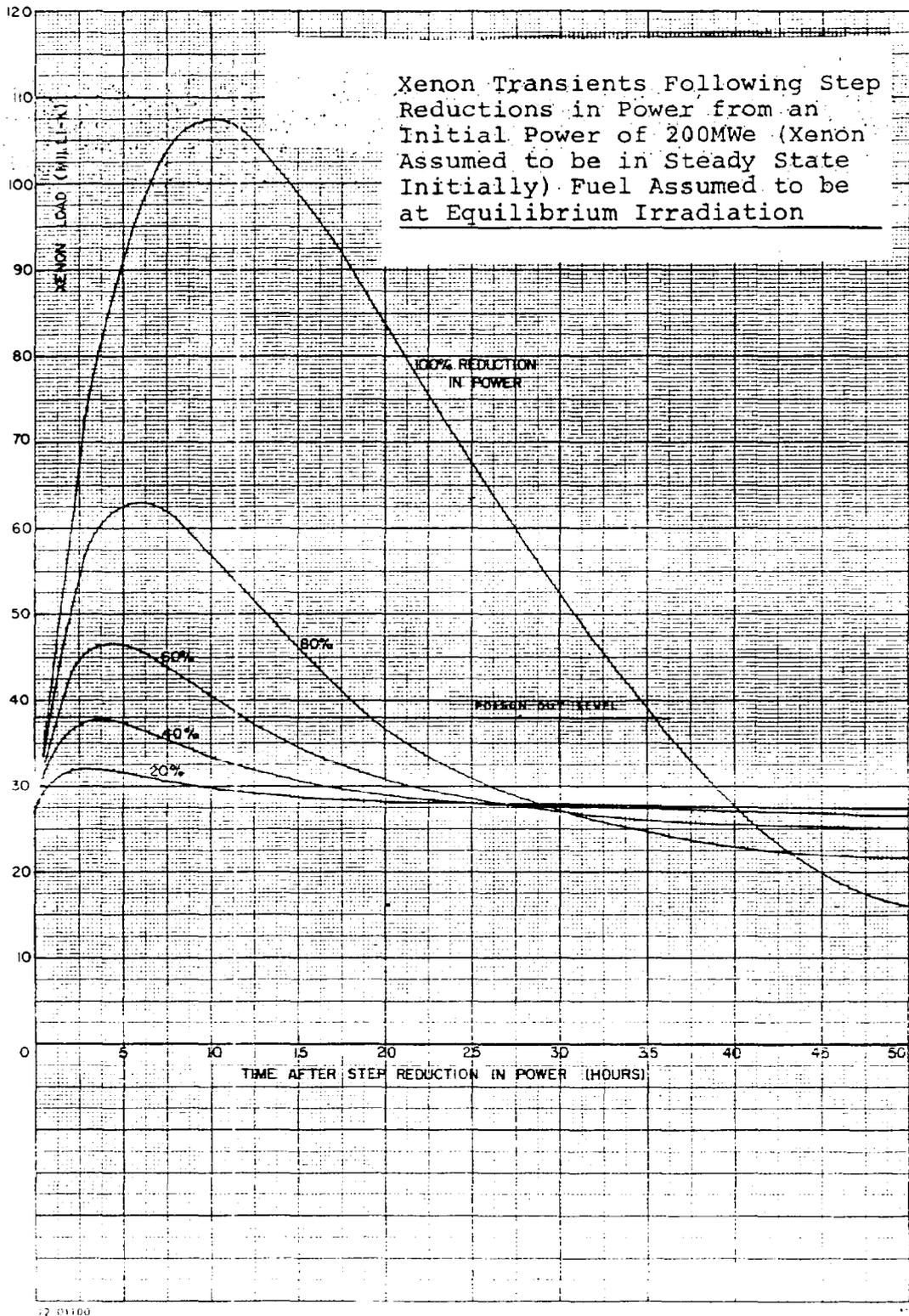
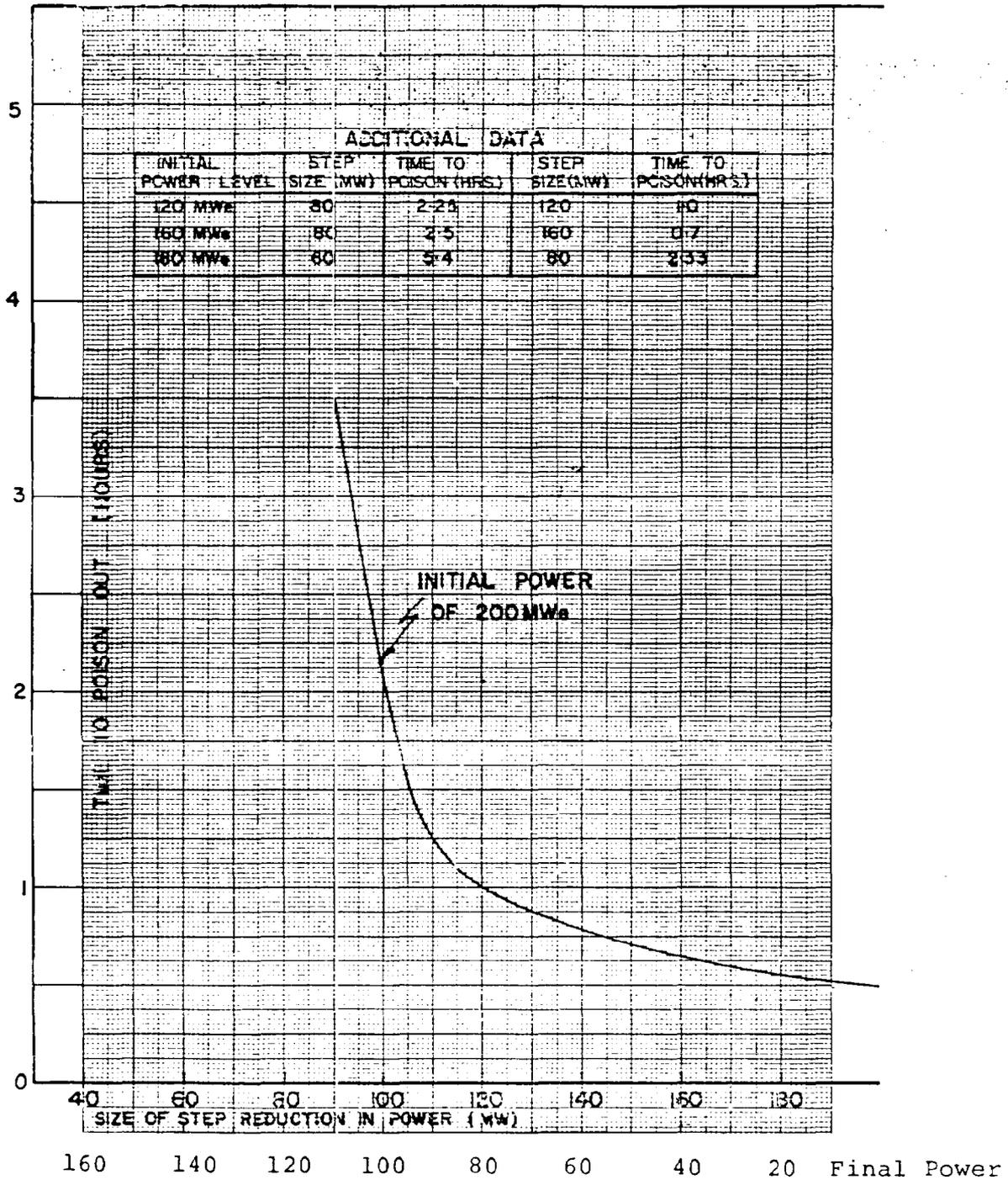
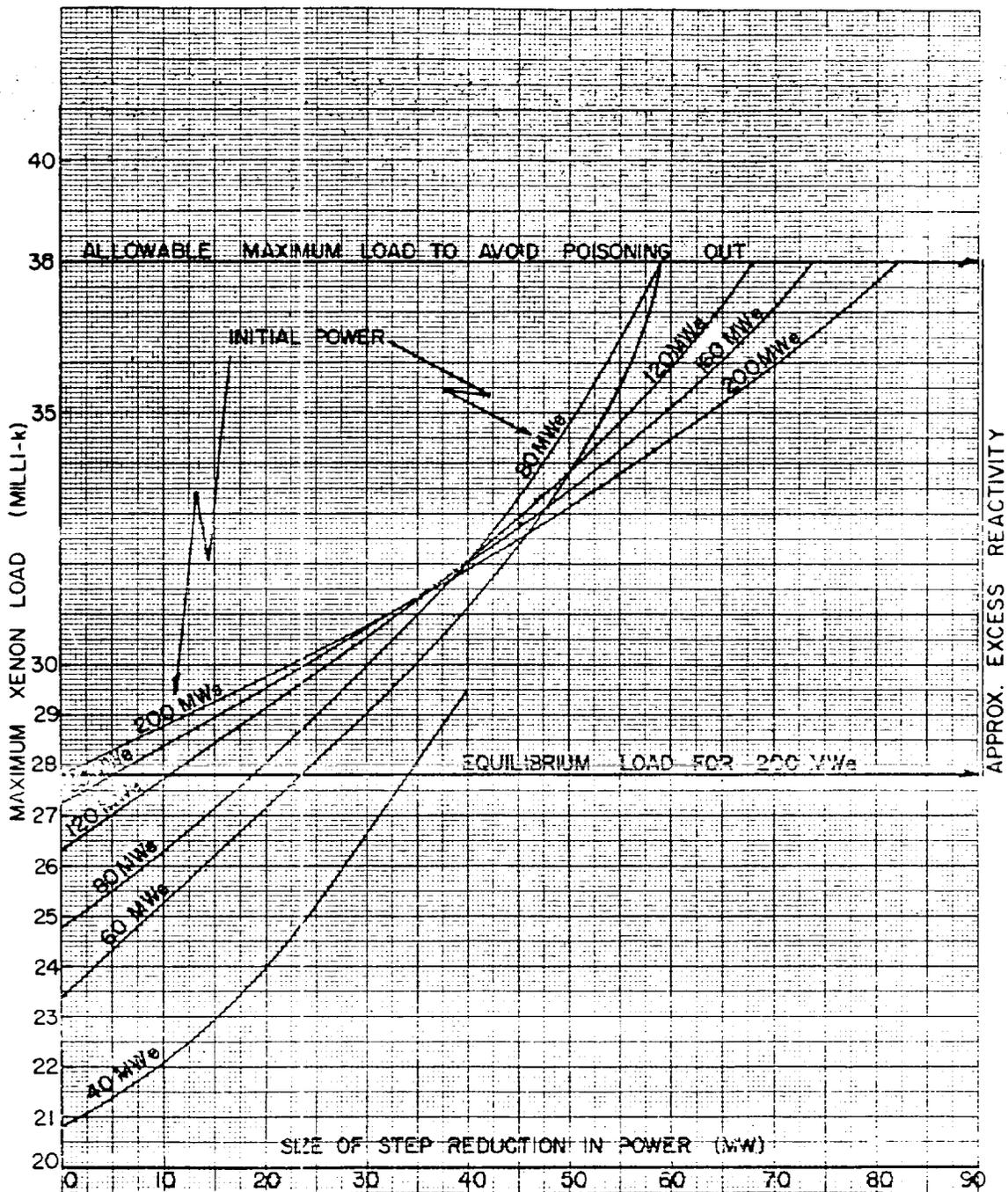


Figure 5



Time to Poison Versus Size of Step Reduction in Power from an Initial Power Level of 200 MWe. Values for Other Initial Power Levels are Shown in Tabular Form. Fuel Assumed to be at Equilibrium Irradiation.



Maximum Xe load attained during the transient following step reductions in power from various initial power levels. (Xenon Assumed to be at the Corresponding Steady State Value Initially; Fuel Assumed to be at Equilibrium Irradiation).

Figure 7

removal by neutron capture will also decrease by 40% from its full power value, but because xenon is still being removed the transient will not reach its shut-down peak. Looking at the figure, you will see that for a 40% reduction the available excess reactivity of  $\sim 10$  mk is just sufficient to override the transient altogether. Ultimately equilibrium will be restored and the xenon load will then be that corresponding to 60% of the full power flux. The figure also shows that the rate of xenon build-up is less for a 60% reduction than for a 100% reduction, and that the poison override time would therefore be longer.

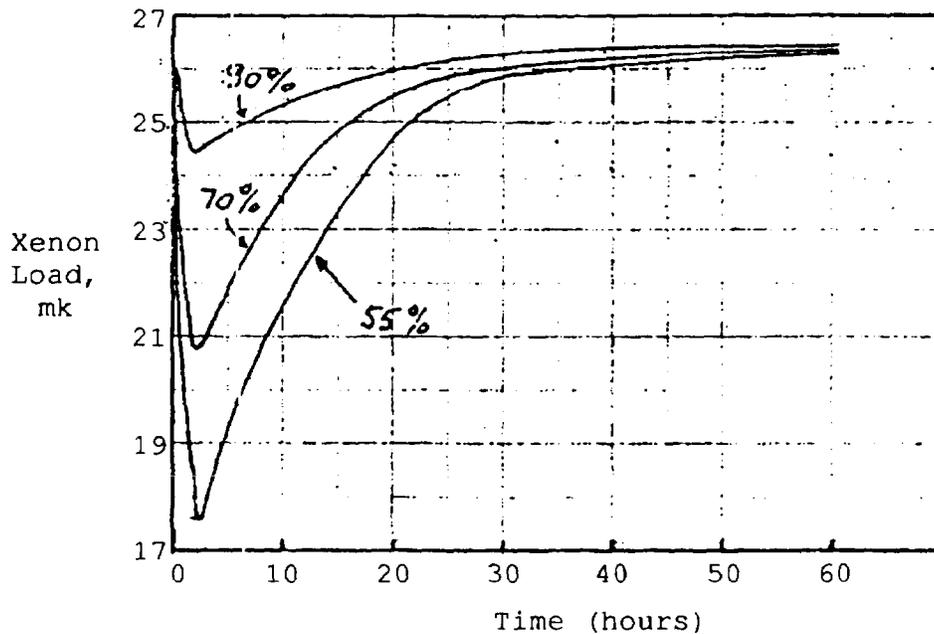
Fig. 6 - shows that this is true, namely that for a fixed amount of excess reactivity the poison override time depends on the size of the power reduction. For example, the curve shows that for a reduction of 120 MWe this time will be 1 hour, but it will be twice that for a reduction of 100 MWe.

Fig. 7 - shows the maximum xenon loads reached during the transient following step reductions from various initial power levels. For example, if the reactor is operating at 160 MWe and is then taken down to 100 MWe, the xenon load will increase from 27.2 mk to 35.1 mk. With 10 mk excess reactivity there should be no problem, but without looking at curves like this you wouldn't know whether there would be.

The converse to these curves also applies. For example, if the reactor is running at 140 MWe (at equilibrium) and it is taken to 200 MWe, the immediate effect will be a gain in reactivity due to increased burnup of xenon. At the same time more iodine will be produced which will not show up as extra xenon production until later on. As a result, the curve will run through a minimum, and then the xenon production will increase because of the increasing amount of iodine that is decaying. Eventually, the xenon concentration will attain the new equilibrium value corresponding to operation at 200 MW. The whole process is shown schematically in Fig. 8, and it does not normally present any operational problems.

### Xenon Oscillations

So far, we have assumed that the xenon poisoning and reactivity loads apply to the reactor as a whole. No mention has been made of the possibility of localized changes in xenon poisoning which can have a very important effect on reactor stability.



Xenon transient Following Step load Increase From  
Various Initial Powers to 100% Final Power

Figure 8

For example, let us consider a reactor that has been operated at power long enough for the iodine and xenon concentrations in the fuel to have reached equilibrium.

Suppose now that without changing the total power of the reactor, the flux is increased in one region of the reactor and simultaneously decreased in another region. This change from the desired normal distribution is called a *flux tilt*. This may happen, for example, if a shutoff rod drops into the core, with bulk power control increasing reactor power to maintain it at setpoint (for the purposes of this explanation, we will assume that there is no spatial control within the reactor). In the region of increased flux (away from the inserted shutoff rod), the xenon burns up more rapidly than it did prior to the change, and its concentration decreases. This leads to a higher reactivity in this section of the core, which leads to an increased flux. This again results in the xenon concentration decreasing further due to increased burnup, increasing local reactivity, and so on.....

In the region of decreased flux, the xenon concentration increases due to its reduced burnup, together with the continuing decay of iodine, which was produced in the original higher flux. This increase in xenon concentration lowers the flux even further in this region of the core,

which increases the xenon concentration, which lowers the flux, and so on..... Let's stress here again the fact that the overall reactor power has not changed, and low power from one region in the core is compensated by high power in another region.

Now, these local power excursions do not continue forever. In the region of increased flux, the iodine production increases, hence the production of xenon from iodine decay eventually increases. This causes a reactivity decrease in the high power region of the core.

Similarly, in the region of reduced flux, iodine production decreases as compared to "normal" levels. Hence the production of xenon will be lower than normal. The accumulated xenon eventually decays, increasing the local activity and reversing the power transient in this region as well.

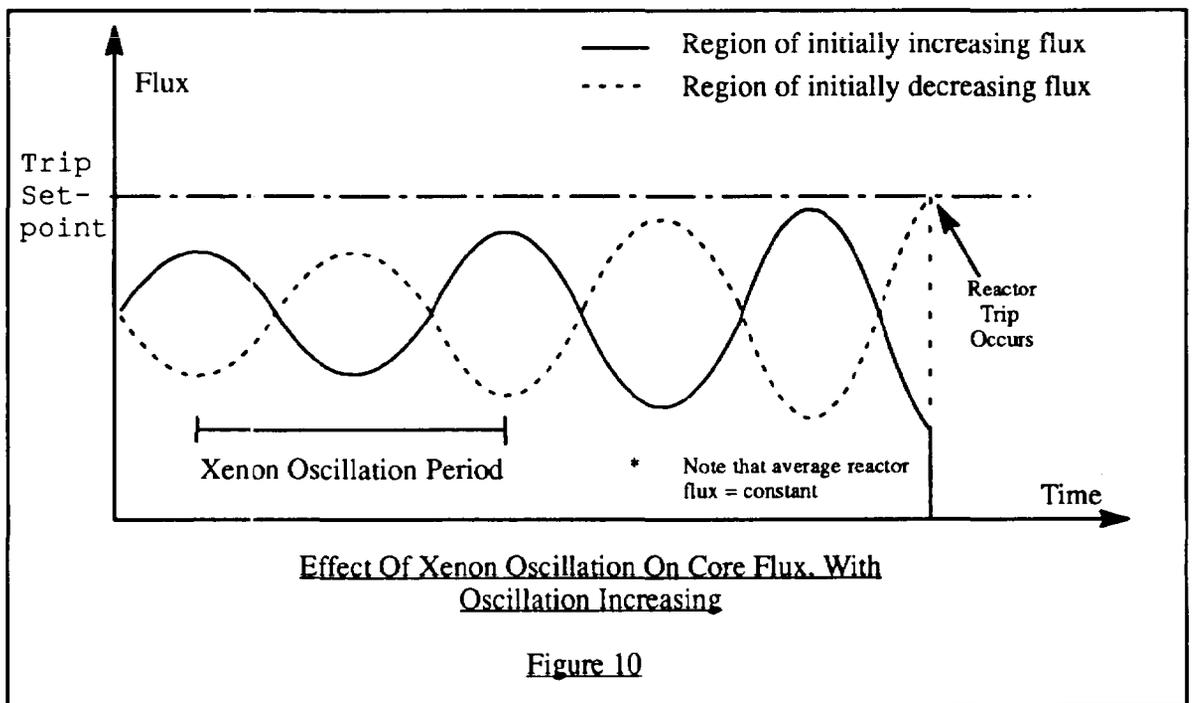
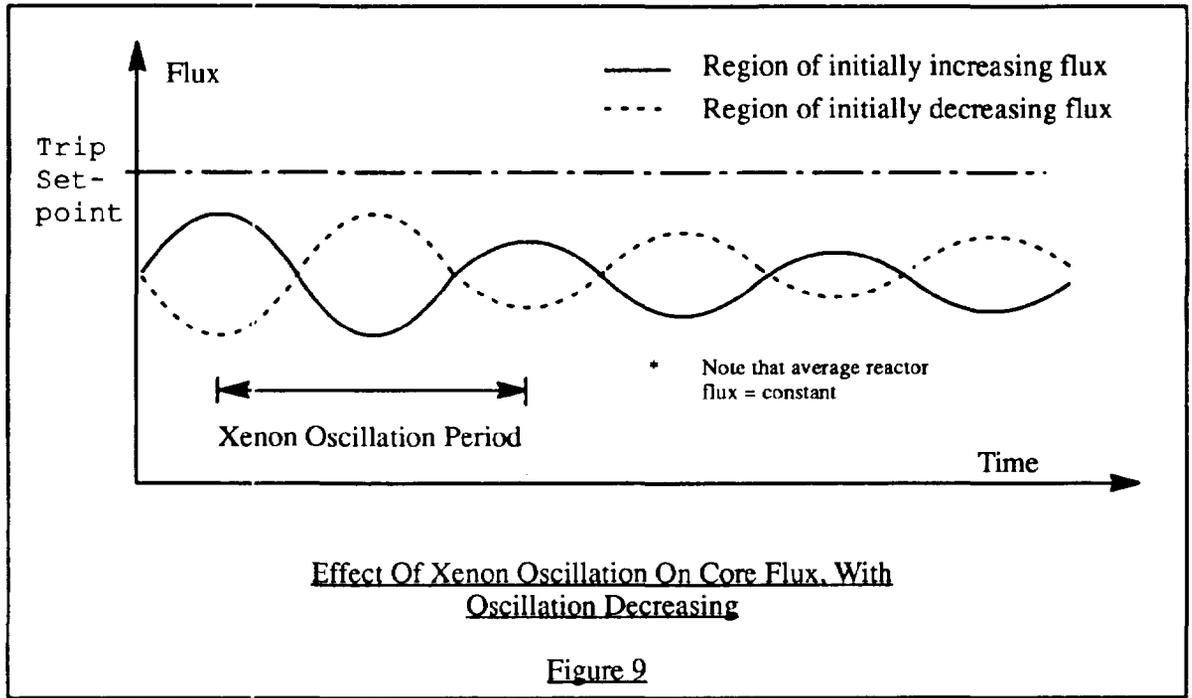
When the power trends in these abnormally powered zones reverse, the reactor flux configuration returns to an apparently "normal" state, but the trend continues. The low power zone will become a high power zone, as the high power zone will become a low power zone. The reason for this is that the xenon and iodine concentrations in these zones still differ from equilibrium values when the "normal" state is reached.

In the zone that was at high power, iodine production has increased above equilibrium levels, and will result in xenon production to values above its equilibrium level. This will result in an overshoot as power decreases to below "normal" values. Similarly, in the low power zone, the iodine production has been lower than equilibrium levels, and will result in xenon production to values below equilibrium levels. This will result in an overshoot as power increases to above "normal" values.

In this way, the flux and power of a reactor may oscillate between different regions (end-to-end, side-to-side) unless action is taken to control them. The *Xenon oscillation period* is the time from the peak to following peak in a given region. The xenon oscillation period can range from about 15 to 30 hours. Also, depending on flux conditions, and reactivity device movements during the transient, the period of the next oscillation may be different than the current or previous one.

Depending on the size of the transient and the response of the regulating system, the oscillation amplitude could either increase or decrease. Figure 9 shows a decreasing amplitude oscillation (indicating the oscillation is under control). Figure 10 shows an increasing amplitude oscillation. Such an operating condition will eventually cause excessively high bundle power in certain regions of the core, which threatens local fuel integrity, and would result in a reactor trip initiated by the regional overpower protection system. If an increasing amplitude oscillation

is detected, reactor power must be reduced in order to minimize additional stress on the fuel, and the possibility of a trip occurring.



Xenon oscillations can only occur in large reactors. The argument to show this is as follows:

If the neutrons produced in one region of the reactor do not cause significant fissions in another region, then the two regions can act independently of one another. The criterion that determines whether or not this is possible is the degree of neutron migration from the one region to the other. In a small reactor, the core is small enough to permit a disturbance started in one region to have an effect in another region. The xenon and flux changes would therefore affect the whole core and a regulating system based on flux measurement in one locality can correct the flux disturbance and prevent xenon oscillations from being initiated.

If the reactor is large, leakage of neutrons between regions is very small. A disturbance started in one region has little effect in another region. Thus, if a flux increase occurs due to a fuel change in one region, for example, a non-regional regulating system would compensate for this and maintain steady power by lowering the flux in another region to keep the average flux across the core constant. This would set up a xenon oscillation in the second region exactly out of phase with that in the first region.

Furthermore, it is obvious that xenon oscillations can only occur if the flux is high enough for xenon burnup to be as pronounced as xenon decay.

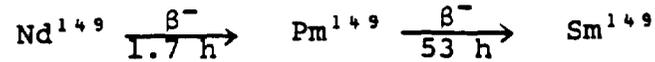
These two conditions for the presence of xenon oscillations (ie, large reactor size and high flux) are satisfied for most power reactors. Since xenon oscillations can occur at constant power they may go unnoticed unless the flux and/or power density distributions are monitored at several points in the reactor. This must be done in order to prevent such oscillations, since they represent something of a hazard to the safe operation of a reactor.

In any event, these oscillations, if permitted to continue, burden the core materials with unnecessary temperature cycling which may result in premature materials failure.

The purpose of the liquid zone control system is to prevent xenon oscillations. Reactors are subdivided into 14 regions (called zones), and each region has its own flux detectors. The output of these detectors is used to adjust the amount of light water absorber in the zone control compartments, controlling local neutron flux.

Samarium-149

Sm-149 is the most important of the stable fission products. It is formed in the fuel by the decay of fission product neodymium-149 and promethium-149:



Since Sm-149 is stable, the only removal process for it is neutron capture. The Sm-150 formed has a low absorption and is therefore insignificant. Sm-149 has a much lower cross section ( $4.2 \times 10^{-6} \text{b}$ ) than Xe-135, it will take correspondingly longer for equilibrium to be reached. The half-life of neodymium is so short compared to promethium that we lump its fission product yield with promethium. Note that there is no direct production of samarium from fission. As with xenon we need two equations to describe the behaviour:

$$\frac{d}{dt} N_{\text{Pm}} = \underbrace{\gamma_{\text{Pm}} \Sigma_f \phi}_{\text{Production from fission}} - \underbrace{\lambda_{\text{Pm}} N_{\text{Pm}}}_{\text{Loss due to decay}}$$

$$\frac{d}{dt} N_{\text{Sm}} = \underbrace{\lambda_{\text{Pm}} N_{\text{Pm}}}_{\text{Production from decay fo Pm}} - \underbrace{\sigma_a^{\text{Sm}} N_{\text{Sm}} \phi}_{\text{Loss due to burnup}}$$

where:  $\gamma_{\text{Pm}}$  = Fission Product Yield of Promethium  
 $\Sigma_f$  = Fission Cross Section of the Fuel  
 $\phi$  = Average Neutron Flux  
 $\lambda_{\text{Pm}}$  = Decay Constant of Promethium  
 $N_{\text{Pm}}$  = Number Density of Promethium  
 $N_{\text{Sm}}$  = Number Density of Samarium  
 $\sigma_a^{\text{Sm}}$  = Cross Section of Samarium

The equilibrium Pm-149 concentration is:

$$N_{Pm} = \frac{\gamma_{Pm} \Sigma f \phi}{\lambda_{Pm}}$$

Just as with iodine-135, the equilibrium concentration of Pm-149 is a direction function of the power level.

The equilibrium concentration of Sm-149 is:

$$N_{Sm} = \frac{\gamma_{Pm} \Sigma f}{\phi_{sm}}$$

Note that equilibrium samarium is independent of the flux level. Equilibrium Samarium Load is around -5.5 mk and it takes about 300 hours of operation to reach equilibrium for our reactors (time to reach equilibrium is a function of the flux level).

#### Samarium Growth After Shutdown

After a shutdown the samarium concentration will increase since none is being burned out and some is still being produced by the decay of Promethium. The maximum Samarium Load after shutdown depends on the promethium concentration prior to shutdown. For our larger reactors the maximum Samarium Load is about 12 mk. The buildup is shown in Figure 11.

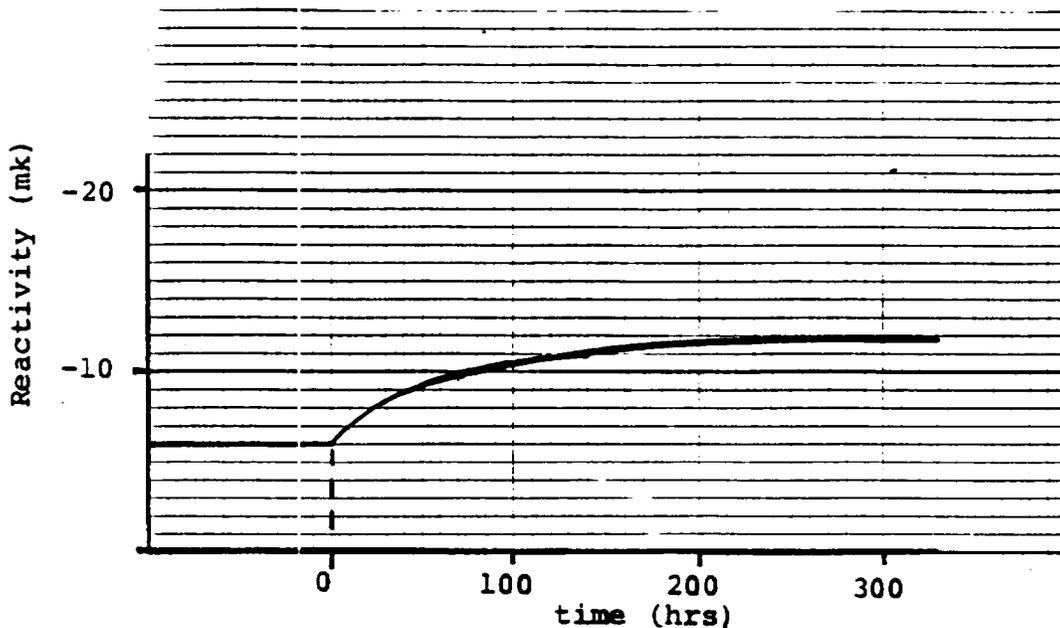


Figure 11

It is interesting to note that although the equilibrium samarium load has to be allowed for in reactor design, the shutdown load may be ignored. There are two reasons for this.

- (1) By looking at the time scale of Fig. 11 you will realize that the maximum samarium load will not appear until the xenon transient has long been and gone. There will therefore be lots of reactivity available. You can also see that the increase in samarium load during the xenon poison override time is negligible, so that this doesn't present a problem either.
- (2) The rate at which the samarium is formed is governed by the Pm-149 half-life of 53 hours, and it corresponds almost exactly to the rate at which Pu-239 is formed after a shutdown. (Pu-239 is still produced from Np-239 decay, but it is not being used up since there are no neutrons). It turns out that the increased reactivity from this plutonium transient more than compensates for the increased samarium load. The net change after shutdown is about +6 mk due to combined effect of samarium and plutonium.

ASSIGNMENT

1. Write the equations for the time rate of change of  $N_{Xe}$  and  $N_I$ . Explain what each term represents and give the magnitudes of the terms. Note the conditions under which these magnitudes are applicable.
2. Explain why equilibrium Xenon Load changes very little when power is raised from 50% to 100%.
3. Explain why peak xenon after shutdown from 100% equilibrium will be nearly twice what it is after shutdown from 50% equilibrium.
4. Give and explain the conditions required for a xenon oscillation to occur.
5. Define Iodine load and explain its significance.
6. Explain why samarium growth after shutdown may be neglected in reactor design.

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